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# SOLUBILITY PARAMETERS OF GAS CHROMATOGRAPHIC MIXED STATIONARY PHASES

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#### SUMMARY

Gas chromatography was used to measure activity coefficients,  $\Omega^{\infty}$ , partial molar free energies of mixing,  $\Delta \bar{G}_1^{\infty}$ , Flory-Huggins interaction parameters,  $\chi^{\infty}$ , and its enthalpic and entropic contributions, of a number of solutes on five single and fourteen mixed stationary phases at 120°C. Solubility parameters of the stationary phases,  $\delta_2$ , were deduced by the method of DiPaola-Baranyi and Guillet for the different solute-stationary phase combinations. The polymer-polymer interaction parameter,  $\chi'_{2,3}$ , was also calculated for the various mixed systems.

#### INTRODUCTION

One of the problems with which the chromatographer is faced is to find a column with an appropriate selectivity for separating the components of the mixture to be analysed. Basically there are three procedures that can be used to modify the selectivity of the chromatographic column if no commercial stationary phase that can perform the separation is available: to synthesize new stationary phases with functional groups capable of producing the desired effect, to use columns coupled in series or to use mixtures of stationary phases in the same chromatographic column. Mixed stationary phases are particularly useful in connection with work with open-tubular columns, bearing in mind that there are few stationary phases with the necessary characteristics of stability, wettability, etc., which are needed if a long-lasting and efficient column is to be obtained. Some workers think that mixed stationary phase behaviour might easily be predicted from the characteristics of the liquids that are mixed<sup>1-5</sup>. Others, however consider that there is great uncertainty in this matter<sup>1,6-12</sup>. In our opinion, any attempt to predict the chromatographic behaviour of mixed stationary phases must be based on a good knowledge of their thermodynamic properties.

The most popular stationary phases in gas chromatography (GC) are polymers of high molecular weight, often unknown. Thermodynamic characterization of polymers is possible with the use of  $GC^{13}$  and has been greatly facilitated after the work of Patterson *et al.*<sup>14</sup>, who showed that this characterization is possible with the molecular weight of the polymer being ignored. Many papers based on these ideas have been published<sup>15-22</sup>. One such important thermodynamic parameter is the solubility parameter of the stationary phase. Many physical properties are related to this parameter, and it is a general impression that its knowledge may lead to approximate estimates of the chromatographic behaviour of mixed stationary phases.

In this work, solubility parameters at 120°C were calculated for three sets of stationary phases using partial molar free energies of mixing following the procedure described by Price *et al.*<sup>20</sup>. The Flory-Huggins interaction parameter  $\chi^{\infty}$  was also calculated, as together with its enthalpic and entropic contributions,  $\chi_{\rm H}^{\infty}$  and  $\chi_{\rm S}^{\infty}$ . The polymer-polymer interaction parameter  $\chi'_{2,3}$  was evaluated for different mixed stationary phases.

## EXPERIMENTAL

The apparatus, stationary phases, columns and chromatographic procedures have been described previously<sup>12</sup>. The same mixtures of OV-101–OV-25, OV-101–Carbowax 20M and OV-225–SP-2340 were used.

# **RESULTS AND DISCUSSION**

# Activity coefficients

Activity coefficients at infinite dilution based on the weight fraction,  $\Omega_1^{\infty}$ , were calculated<sup>14,20</sup> using the equation

$$\ln \Omega_1^{\infty} \equiv \ln \frac{a_1}{w_1} = \ln \left( \frac{273.15 R}{P_1^0 V_g^0 M_1} \right) - \frac{P_1^0}{RT} (B_{11} - V_1^0)$$
(1)

which has the advantage of ignoring the molecular weight of the polymer. In this equation,  $a_1$  and  $w_1$  are the activity and weight fraction of the solute in the polymer, respectively, and  $M_1$ ,  $P_1^0$ ,  $B_{11}$ ,  $V_1^0$  and  $V_g^0$  are the molecular weight, saturated vapour pressure, second virial coefficient, molar volume and specific retention volume of the solute at the column temperature T, respectively.

Vapour pressures were deduced using Antoine coefficients from various sources<sup>23,24</sup>. The second virial coefficients of *n*-nonane, *n*-decane and *n*-dodecane were calculated by the procedure of O'Connell and Prausnitz<sup>25</sup>; for other solutes, values were extrapolated from literature values corresponding to other temperatures<sup>26</sup>. Densities at 393 K were calculated according to the pertinent equation<sup>27</sup>. No data were found for six of the ten solutes used by McReynolds to characterize stationary phases<sup>28</sup>. Molar volumes were calculated from molecular weight and density values. Molar enthalpies of vaporization were deduced from data published at various temperatures<sup>7,23,29,30</sup>. Values at 393 K are shown in Table I.

Activity coefficients of the various solutes in the different stationary phases (single and mixed) found according to eqn. 1 are shown in Table II.

Solute	P <sup>0</sup> (Torr)	- B <sub>11</sub> (1 mol <sup>-1</sup> )	$\rho_1 \ (g \ ml^{-1})$	V <sup>0</sup> (ml mol <sup>-1</sup> )	∆H <sub>v</sub> (cal mol <sup>-1</sup> )	δ <sub>1</sub> [(cal ml <sup>-1</sup> ) <sup>‡</sup> ]
<i>n</i> -Hexane	2984.49	0.895	0.5450	158.13	6125	5.81
n-Heptane	1373.88	1.285	0.5924	169.16	7263	6.19
n-Octane	647.74	1.785	0.6170	185.14	8327	6.38
n-Nonane	310.89	2.439	0.6368	201.43	9465	6.57
n-Decane	151.27	3.106	0.6536	217.70	10610	6.72
<i>n</i> -Undecane	74.34	3.935	0.6660	234.71	11750	6.84
n-Dodecane	36.89	5.102	0.6761	251.96	12650	6.86
n-Tridecane	18.25	6.362	0.6861	268.72	13750	6.95
n-Tetradecane	9.17		0.6940	285.88	14800	7.00
n-Pentadecane	4.59		0.6988	303.98	16010	7.08
Benzene	2249.31	0.74	0.7681	101.71	6950	7.79
1-Butanol	823.27	1.055	0.7354	100.79	10255	9.69
2-Pentanone	1259.22	1.29	0.7043	122.30	7720	7.53
Pyridine	870.96	0.97	0.8873	89.15	8323	9.21

PHYSICAL PROPERTIES OF SOLUTES AT 393 K

TABLE I

## The solute-polymer interaction parameter

The Flory-Huggins solute-polymer interaction parameter may be calculated from activity coefficients<sup>14,20,\*</sup>. In the case of pure solvents the equation is

$$\chi_{1,2}^{\infty} = \ln \Omega_1^{\infty} + \ln \frac{\rho_1}{\rho_2} - \left(1 - \frac{V_1^0}{V_2^0}\right)$$
(2)

where  $\rho_1$  and  $\rho_2$  are the densities of the solute (1) and the polymer (2) and  $V_1^0$  and  $V_2^0$  the corresponding molar volumes. When the polymer is in fact a mixture of two polymers (mixed stationary phases) the equation becomes<sup>15,31,32</sup>

$$\chi_{1,(2,3)}^{\infty} = \ln \Omega_1^{\infty} + \ln \frac{\rho_1}{\rho_m} - \left(1 - \frac{V_1^0}{V_2^0}\right) \varphi_2 - \left(1 - \frac{V_1^0}{V_3^0}\right) \varphi_3$$
(3)

where  $\rho_m$  is the density of the mixture of polymers,  $V_2^0$  and  $V_3^0$  are the molar volumes of the two polymers and  $\varphi_2$  and  $\varphi_3$  the corresponding volume fractions in the mixture. As  $V_2^0$  and  $V_3^0$  are much larger than  $V_1^0$ , the use of both equations is greatly simplified.

Values of the solute-polymer interaction parameters corresponding to the different solutes in the various stationary phases are presented in Table III. Comparing values of  $\chi^{\infty}$  corresponding to *n*-alkanes with the corresponding values of the partition coefficients ( $K_R$ ) for the same mixtures<sup>12</sup>, it may be observed that even in the set of mixtures where values of  $K_R$  may be said to show a "quasi"-linear behaviour with mixture composition (OV-101-OV-25), the same type of behaviour may not be observed in the case of the  $\chi^{\infty}$  values.

<sup>\*</sup> There is a transcription error in eqn. 3 in ref. 20. The authors used the correct equation in their calculations.

# TABLE II

# ACTIVITY COEFFICIENTS AT 393 K ON DIFFERENT STATIONARY PHASES

Compound	<i>φον</i> -101							
	1	0.831	0.589	0.410	0.397	0.268	0.084	0
n-Hexane	4.70	5.18	6.30	7.70	7.70	8.40	10.90	11.57
<i>n</i> -Heptane	5.10	5.63	6.85	8.39	8.37	9.17	11.89	12.68
n-Octane	5.43	5.95	7.35	9.02	8.99	9.86	12.85	13.73
n-Nonane	5.76	6.32	7.78	9.54	9.56	10.52	13.71	14.68
n-Decane	6.05	6.67	8.20	10.11	10.12	11.17	14.54	15.75
n-Undecane	6.38	7.01	8.66	10.72	10.68	11.82	15.41	16.74
n-Dodecane	6.70	7.34	9.13	11.31	11.27	12.49	16.26	17.77
Benzene	4.69	4.62	4.63	4.74	4.85	4.82	5.02	4.85
1-Butanol	14.62	14.48	15.48	16.06	16.65	16.64	18.09	17.14
2-Pentanone	7.04	6.64	6.96	7.14	7.45	7.00	7.52	7.33
Pyridine	6.85	7.18	5.81	5.56	6.03	5.68	5.52	5.24

## Mixtures of OV-101-OV-25

Mixtures of OV-101-Carbowax 20M

Compound	<i>φον</i> -101					
	1	0.757	0.509•	0.257	0	
n-Hexane	4.70	6.54	9.61	14.95	25.77	
n-Heptane	5.10	7.11	10.53	16.61	31.01	
n-Octane	5.43	7.68	11.29	18.06	34.93	
n-Nonane	5.76	8.18	12.15	19.57	40.09	
n-Decane	6.05	8.68	13.02	21.08	45.48	
n-Undecane	6.38	9.17	13.85	22.81	51.91	
n-Dodecane	6.70	9.69	14.68	24.51	58.68	
Benzene	4.69	5.54	5.69	6.05	5.58	
1-Butanol	14.62	12.94	9.74	7.83	6.54	
2-Pentanone	7.04	8.24	7.92	7.53	6.68	

# Mixtures of OV-225-SP-2340

Compound	<i>φov-</i> 225							
	1	0.781	0.508	0.363	0.327	0.103	0	
<i>n</i> -Hexane	11.46	12.61	15.94	24.85	25.28	41.30	59.95	
n-Heptane	13.03	14.35	18.45	29.06	29.29	50.10	74.39	
n-Octane	14.52	15.99	21.22	33.46	33.96	60.11	91.68	
n-Nonane	16.09	17.90	23.87	38.10 <sup>,</sup>	39.19	71.59	110.99	
n-Decane	17.71	19.94	26.91	43.69	44.70	85.44	134.53	
n-Undecane	19.51	21.87	30.08	48.99	50.87	100.69	162.91	
n-Dodecane	21.37	24.09	33.67	55.88	57.81	117.12	196.58	
n-Tridecane	23.56	26.69	37.89	63.51	65.77	140.88	237.91	
n-Tetradecane*	25.71	29.24	42.29	71.50	74.42	166.16	285.56	
n-Pentadecane*	28.53	32.59	47.87	81.77	85.51	198.80	346.19	
Benzene	4.12	4.08	4.01	5.20	4.50	5.68	6.98	
1-Butanol	8.00	7.35	6.59	7.95	6.97	7.91	9.69	
2-Pentanone	4.23	4.18	4.10	6.19	4.57	6.60	8.22	
Pyridine	3.72	3.37	3.02	3.80	3.18	3.58	4.37	

# TABLE III

# SOLUTE-POLYMER INTERACTION PARAMETERS ( $\chi^\infty)$ AT 393 K

Mixtures of OV-101-OV-25

Compound	<i>φov</i> -101							
	1	0.831	0.589	0.410	0.397	0.268	0.084	0
<i>n</i> -Hexane	0.044	0.102	0.248	0.412	0.409	0.471	0.696	0.741
<i>n</i> -Heptane	0.208	0.269	0.415	0.581	0.577	0.643	0.867	0.915
n-Octane	0.313	0.365	0.526	0.694	0.688	0.755	0.985	1.036
n-Nonane	0.401	0.458	0.614	0.782	0.781	0.852	1.082	1.134
n-Decane	0.477	0.538	0.693	0.866	0.864	0.938	1.167	1.231
<i>n</i> -Undecane	0.550	0.606	0.766	0.943	0.937	1.014	1.243	1.310
n-Dodecane	0.613	0.666	0.834	1.012	1.006	1.083	1.312	1.386
Benzene	0.385	0.332	0.282	0.269	0.290	0.258	0.263	0.214
1-Butanol	1.478	1.430	1.446	1.446	1.480	1.454	1.503	1.433
2-Pentanone	0.704	0.607	0.604	0.592	0.633	0.546	0.582	0.540
Pyridine	0.908	0.917	0.654	0.574	0.652	0.567	0.504	0.436

# Mixtures of OV-101-Carbowax 20M

Compound	<i>φον</i> -101					
	1	0.757	0.509	0.257	0	
n-Hexane	0.044	0.321	0.655	1.048	1.544	 
n-Heptane	0.208	0.487	0.829	1.237	1.813	
n-Octane	0.312	0.606	0.940	1.361	1.973	
n-Nonane	0.401	0.700	1.045	1.473	2.142	
n-Decane	0.476	0.786	1.141	1.573	2.294	
n-Undecane	0.550	0.860	1.221	1.671	2.445	
n-Dodecane	0.613	0.930	1.294	1.758	2.583	
Benzene	0.385	0.498	0.474	0.487	0.358	
1-Butanol	1.478	1.303	0.968	0.700	0.472	
2-Pentanone	0.704	0.809	0.718	0.618	0.451	

# Mixtures of OV-225-SP-2340

Compound	<i>φ</i> ov-225							
	1	0.781	0.508	0.363	0.327	0.103	0	
n-Hexane	0.776	0.865	1.089	1.529	1.544	2.028	2.397	
n-Heptane	0.988	1.077	1.319	1.769	1.775	2.304	2.696	
n-Octane	1.137	1.226	1.499	1.950	1.964	2.527	2.946	
n-Nonane	1.272	1.370	1.649	2.112	2.139	2.734	3.169	
n-Decane	1.394	1.504	1.795	2.275	2.296	2.937	3.387	
n-Undecane	1.509	1.615	1.925	2.408	2.444	3.120	3.597	
n-Dodecane	1.615	1.727	2.053	2.555	2.587	3.286	3.800	
n-Tridecane	1.727	1.844	2.186	2.697	2.731	3.485	4.006	
n-Tetradecane*	1.826	1.947	2.307	2.827	2.866	3.662	4.200	
n-Pentadecane*	1.937	2.063	2.438	2.968	3.012	3.848	4.399	
Benzene	0.096	0.080	0.053	0.307	0.163	0.387	0.590	
1-Butanol	0.716	0.624	0.507	0.689	0.556	0.674	0.874	
2-Pentanone	0.035	0.016	-0.013	0.395	0.089	0.451	0.666	
Pyridine	0.137	0.031	-0.086	0.139	-0.040	0.069	0.265	

#### The solubility parameter

According to the Hildebrand-Scatchard theory, the solubility parameter of a substance is defined as the square root of the cohesive energy density, defined as the ratio of the energy of vaporization to the molar volume, both at the same temperature:

$$\delta \equiv (\Delta E_{\rm v}/V_1^0)^{\frac{1}{2}} \tag{4}$$

When two liquids are mixed the difference between the two solubility parameters  $(\delta_1 \text{ and } \delta_2)$  is given<sup>29</sup> by the expression

$$\delta_1 - \delta_2 = (\Delta E_{\rm m}/\varphi_1 \varphi_2 V_{\rm m})^{\frac{1}{2}} \tag{5}$$

where  $\Delta E_{\rm m}$  is the energy of mixing of the two liquids at constant volume,  $\varphi_1$  and  $\varphi_2$  are the volume fractions of the components and  $V_{\rm m}$  is the average molar volume based on molar fraction. Solubility parameters have been useful in describing the thermodynamic properties of dilute solutions and have been shown to be related to a number of physical properties of polymers such as surface tension, wettability and glass transition temperature. Solubility parameters of substances at a given temperature T may be calculated with the expression

$$\delta_1 = \left(\frac{\Delta H_v - RT}{V_1^0}\right)^{\frac{1}{2}} \tag{6}$$

where  $\Delta H_v$  is the molar enthalpy of vaporization of the substance at temperature T and R is the universal gas constant. In this way  $\delta$  values at 120°C were calculated for the various solutes used in this work and are shown in the last column in Table I.

Polymers have very low vapour pressures and therefore it is not possible to calculate  $\delta_2$  directly using eqn. 6. However, Guillet<sup>13</sup> has shown that gas-liquid chromatography is ideal for determining this parameter at a given temperature. Two methods<sup>29</sup> were used in this work to calculate values of  $\delta_2$  for the different mixtures of the three sets of stationary phases studied. One is based on the molar partial free energy of mixing,  $\Delta \bar{G}_1^{\infty}$ , and the other on the Flory-Huggins interaction parameter,  $\chi^{\infty}$ . Assuming zero volume change on mixing, eqn. 5 may be written in terms of the partial molar heat of mixing  $(\Delta \bar{H}_1^{\infty})^{29}$ :

$$\Delta \bar{H}_{1}^{\infty} = V_{1}^{0} (\delta_{1} - \delta_{2})^{2}$$
<sup>(7)</sup>

At constant pressure, it is the free energy and not the heat of mixing that is given directly by the solubility parameters<sup>29,33</sup>, and eqn. 7 therefore becomes

$$\Delta \bar{G}_{1}^{\infty} = V_{1}^{0} \left( \delta_{1} - \delta_{2} \right)^{2} \tag{8}$$

The partial molar free energy of mixing was evaluated<sup>29</sup> from the expression

$$\Delta \bar{G}_1 = RT \ln \Omega_1^{\infty} \tag{9}$$

# TABLE IV

# PARTIAL MOLAR FREE ENERGIES OF MIXING ( $\Delta \bar{G}_1^{\infty}$ , cal mol<sup>-1</sup>) AT 393 K

Mixtures o	of 0	V-10	1-0	V-25
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Compound	<i>Фо</i> г-101							
	1	0.831	0.589	0.410	0.397	0.268	0.084	0
n-Hexane	1209	1284	1438	1595	1595	1663	1866	1913
n-Heptane	1273	1350	1503	1662	1660	1732	1934	1984
n-Octane	1323	1393	1558	1718	1716	1788	1995	2047
n-Nonane	1367	1441	1602	1762	1764	1839	2046	2099
n-Decane	1406	1483	1644	1807	1808	1885	2091	2154
n-Undecane	1448	1521	1686	1853	1850	1930	2137	2201
n-Dodecane	1486	1557	1728	1895	1892	1973	2179	2248
Benzene	1208	1196	1197	1215	1234	1228	1260	1234
1-Butanol	2096	2088	2140	2169	2197	2197	2262	2220
2-Pentanone	1525	1479	1516	1535	1569	1521	1576	1556
Pyridine	1504	1540	1375	1341	1404	1357	1335	1294

# Mixtures of OV-101-Carbowax 20M

Compound	<i>φον</i> -101					
	1	0.757	0.509	0.257	0	
n-Hexane	1209	1467	1768	2113	2538	
n-Heptane	1273	1532	1839	2195	2683	
n-Octane	1322	1593	1894	2261	2776	
n-Nonane	1367	1642	1951	2323	2884	
n-Decane	1406	1689	2005	2382	2982	
n-Undecane	1448	1732	2053	2443	3086	
n-Dodecane	1486	1775	2099	2499	3181	
Benzene	1208	1338	1358	1407	1344	
1-Butanol	2096	2000	1779	1608	1467	
2-Pentanone	1525	1648	1617	1577	1484	

# Mixtures of OV-225-SP-2340

Compound	<i>φov</i> -225							
	1	0.781	0.508	0.363	0.327	0.103	0	
<i>n</i> -Hexane	1906	1980	2163	2510	2523	2907	3198	
n-Heptane	2006	2081	2277	2632	2638	3058	3367	
n-Octane	2090	2166	2387	2742	2754	3200	3530	
n-Nonane	2171	2254	2479	2844	2866	3337	3679	
n-Decane	2246	2338	2572	2951	2969	3475	3830	
n-Undecane	2321	2410	2659	3040	3070	3603	3979	
n-Dodecane	2392	2486	2747	3143	3170	3721	4126	
n-Tridecane	2469	2566	2840	3243	3270	3866	4275	
n-Tetradecane*	2537	2637	2926	3336	3367	3995	4418	
n-Pentadecane*	2618	2722	3022	3441	3476	4135	4568	
Benzene	1106	1099	1085	1287	1176	1357	1518	
1-Butanol	1624	1558	1474	1620	1517	1615	1774	
2-Pentanone	1126	1117	1102	1424	1186	1475	1645	
Pyridine	1025	948	864	1044	905	996	1152	

Values of  $\Delta \vec{G}_1^{\infty}$  for the different solutes and mixtures are presented in Table IV. Rearranging eqn. 8, values of  $[\delta_1^2 - (\Delta \vec{G}_1^{\infty}/V_1^0)]$  may be plotted versus  $\delta_1$ . The slope of the straight line obtained is twice the solubility parameter of the polymer,  $\delta_2$ .

A second method, based on the procedure developed by Guillet and coworkers<sup>20,29</sup>, was used to evaluate solubility parameters of the various stationary phases at 120°C. Combining the Flory treatment<sup>34</sup> with Hildebrand–Scatchard theory and bearing in mind that the interaction parameter has free energy characteristics with enthalpic ( $\chi_{\rm H}^{\infty}$ ) and entropic ( $\chi_{\rm S}^{\infty}$ ) contribution terms, the following expression may be written<sup>20</sup>:

$$\chi^{\infty} = \frac{V_1^0 (\delta_1 - \delta_2)^2}{RT} + \chi_{\rm S}^{\infty}$$
(10)

This equation may be rewritten as

$$\frac{\delta_1^2}{RT} - \frac{\chi^{\infty}}{V_1^0} = \frac{2 \,\delta_2}{RT} \cdot \delta_1 - \left(\frac{\delta_2^2}{RT} + \frac{\chi^{\infty}_s}{V_1^0}\right) \tag{11}$$

Representation of the term in the left-hand side of eqn. 11 versus  $\delta_1$  will yield a straight line whose slope will allow an estimation of  $\delta_2$ . Fig. 1 shows such plots for a few mixed stationary phases. In all instances (20 stationary phases) an excellent linear correlation was found (regression coefficients >0.99). Values of the solubility parameter of the stationary phases at 120°C calculated according to eqns. 8 and 11 are given in Table V for the different mixtures investigated. The value obtained with eqn. 11 is slightly higher than that corresponding to eqn. 8 in all instances. Representation of the rearranged eqn. 8 allows the estimation of the solubility parameter of the stationary phase from the intercept of the straight line. The values so deduced are much closer to those obtained with eqn. 11. Comparing their results with literature values,



Fig. 1. Estimation of solubility parameter ( $\delta_2$ ) of mixed stationary phases from  $\chi$  (eqn. 11). (a) OV-101/OV-25 = 0.831:0.169; (b) OV-101/Carbowax 20M = 0.509:0.491; (c) OV-225/SP-2340 = 0.363:0.637.

DiPaola-Baranyi and Guillet<sup>29</sup> arrived at the conclusion that in their case the procedure based on  $\chi$  gave better results. In the present instance there are no reported values to compare at 120°C, so we cannot say that one of the methods is better than the other. In any event, the values are sufficiently close to each other to make us think that the values are not far from correct.

Fig. 2 shows the variation of the solubility parameter  $\delta_2$  of the various stationary phases in the three systems studied, as deduced with the help of eqn. 11. For curves a and b the values corresponding to a volume fraction of 1 (polymer OV-101 in both instances) are slightly different because the number of solutes used to calculate it is not the same (see Tables III and IV). The general shape of the curves resembles that of the partition coefficients of *n*-alkanes corresponding to the same mixed systems<sup>12</sup>. Except perhaps for curve a, it may be said that solubility parameters of mixtures of polymers may not be deduced as a linear combination of those corresponding to the pure components.

# Enthalpic and entropic contributions to the solute-polymer interaction parameter

Once the solubility parameter of the stationary phase has been found, eqn. 10 may be used to calculate the enthalpic and entropic contributions to the solute-polymer interaction parameter ( $\chi^{\infty} = \chi^{\infty}_{H} + \chi^{\infty}_{S}$ ).  $\chi^{\infty}_{S}$  can also be found from the intercept of the straight line defined by eqn. 11. Table VI presents the values obtained for  $\chi^{\infty}_{H}$  for the various solutes on the different stationary phases. The values of  $\chi^{\infty}_{S}$  deduced from the representation of eqn. 11 (Fig. 1) are given in Table VII. The value of  $\chi^{\infty}_{S}$  obtained by difference between the values shown in Tables III and VI is generally higher than that obtained from eqn. 11 (Table VII). As an example, Table VIII shows the differences corresponding to one mixed stationary phases (OV-101/OV-25 = 0.397/0.603). All three systems of mixed stationary phases show similar



Fig. 2. Variation of the solubility parameter  $\delta_2$  (eqn. 11) of the stationary phase with mixture composition. (a) OV-101–OV-25; (b) OV-101–Carbowax 20M; (c) OV-225–SP-2340.  $\varphi_2$  represents the volume fraction of the first polymer in each instance.

SOLUBILITY P	ARAMETERS O	F STATIONARY	PHASES, δ <sub>2</sub> [(cal	mol <sup>-1</sup> ) <sup>‡</sup> ], AT 393	K			
Mixtures of OV-	101-0V-25							
Equation	Ø0V-101							
	1	0.831	0.589	0.410	0.397	0.268	0.084	0
Eqn. 8 $(A\vec{G}_1^{\infty})$ Eqn. 11 $(\chi_1^{\infty})$	$5.92 \pm 0.19$ $6.46 \pm 0.12$	$5.98 \pm 0.17$ $6.54 \pm 0.10$	$\begin{array}{c} 6.21 \pm 0.18 \\ 6.80 \pm 0.14 \end{array}$	$6.35 \pm 0.18$ $6.97 \pm 0.16$	6.28 ± 0.18 6.90 ± 0.15	6.39 ± 0.18 7.02 ± 0.16	$6.53 \pm 0.20$ 7.19 $\pm 0.19$	$6.65 \pm 0.19$ $7.32 \pm 0.21$
Mixtures of OV-	101-Carbowax 20	М						
Equation	Ø0V-101							
	I I	0.757	0.509	0.257	0			
Eqn. 8 $(\underline{AG}_1^{\infty})$ Eqn. 11 $(\chi_1^{\infty})$	5.85 ± 0.24 6.37 ± 0.14	$6.16 \pm 0.26$ $6.72 \pm 0.16$	$6.73 \pm 0.23$ $7.32 \pm 0.17$	$7.29 \pm 0.20$ $7.90 \pm 0.18$	$7.99 \pm 0.09$ 8.63 $\pm 0.27$			
Mixtures of OV.	.225-SP-2340							
Equation	POV-225							
	1	0.781	0.508	0.363	0.327	0.103	0	
Eqn. 8 $(\Delta \overline{G}_1^{\infty})$ Eqn. 11 $(\chi_1^{\infty})$	$7.40 \pm 0.11$ 8.10 $\pm 0.23$	7.59 ± 0.11 8.30 ± 0.25	$7.93 \pm 0.12$ 8.64 $\pm 0.29$	$7.95 \pm 0.11$ 8.66 $\pm 0.24$	$8.19 \pm 0.13$ $8.91 \pm 0.30$	$8.41 \pm 0.13$ $9.13 \pm 0.30$	8.43 ± 0.13 9.15 ± 0.29	

64

TABLE V

# E. FERNÁNDEZ-SÁNCHEZ et al

# TABLE VI

# ENTHALPIC CONTRIBUTIONS $(\chi^{\omega}_{H})$ to the solute-polymer interaction parameters at 393 K

Mixtures of OV	Mixtures of OV-101–OV-25										
Compound	φον-101										
	1	0.831	0.589	0.410	0.397	0.268	0.084	0			
n-Hexane	0.085	0.107	0.197	0.272	0.238	0.296	0.385	0.461			
<i>n</i> -Heptane	0.016	0.027	0.081	0.133	0.109	0.151	0.218	0.279			
n-Octane	0.001	0.006	0.041	0.082	0.063	0.097	0.155	0.209			
n-Nonane	0.003	0.000	0.014	0.043	0.028	0.054	0.101	0.148			
n-Decane	0.019	0.009	0.002	0.018	0.009	0.026	0.063	0.102			
n-Undecane	0.042	0.026	0.000	0.006	0.001	0.011	0.038	0.071			
n-Dodecane	0.052	0.033	0.001	0.004	0.000	0.008	0.035	0.068			
Benzene	0.229	0.202	0.127	0.087	0.103	0.076	0.046	0.028			
1-Butanol	1.349	1.283	1.081	0.956	1.009	0.921	0.807	0.726			
2-Pentanone	0.180	0.154	0.084	0.049	0.063	0.041	0.018	0.007			
Pyridine	0.858	0.809	0.659	0.568	0.606	0.542	0.461	0.404			

Mixtures of OV-101-Carbowax 20M

Compound	<i>φov</i> -101					
	1	0.757	0.509	0.257	0	
n-Hexane	0.063	0.165	0.456	0.880	1.605	
n-Heptane	0.007	0.060	0.275	0.633	1.290	
n-Octane	0.000	0.026	0.205	0.543	1.194	
n-Nonane	0.010	0.006	0.145	0.458	1.098	
n-Decane	0.034	0.000	0.099	0.388	1.017	
n-Undecane	0.065	0.004	0.069	0.339	0.966	
n-Dodecane	0.078	0.007	0.066	0.346	1.007	
Benzene	0.261	0.150	0.029	0.002	0.092	
1-Butanol	1.424	1.145	0.731	0.416	0.146	
2-Pentanone	0.211	0.104	0.007	0.021	0.189	

## Mixtures of OV-225-SP-2340

Compound	φογ-225									
	1	0.781	0.508	0.363	0.327	0.103	0			
n-Hexane	1.058	1.246	1.614	1.641	1.937	2.221	2.249			
n-Heptane	0.791	0.960	1.298	1.324	1.600	1.869	1.895			
n-Octane	0.698	0.865	1.202	1.228	1.507	1.781	1.808			
n-Nonane	0.607	0.771	1.106	1.132	1.413	1.690	1.717			
n-Decane	0.532	0.692	1.025	1.051	1.334	1.615	1.643			
n-Undecane	0.480	0.639	0.975	1.001	1.288	1.576	1.604			
n-Dodecane	0.494	0.662	1.016	1.044	1.348	1.653	1.683			
n-Tridecane	0.458	0.625	0.983	1.011	1.321	1.634	1.664			
n-Tetradecane*	0.441	0.612	0.978	1.007	1.328	1.651	1.683			
n-Pentadecane*	0.407	0.577	0.947	0.976	1.302	1.634	1.666			
Benzene	0.013	0.034	0.094	0.099	0.163	0.233	0.240			
1-Butanol	0.328	0.253	0.144	0.138	0.080	0.042	0.039			
2-Pentanone	0.051	0.091	0.191	0.200	0.296	0.398	0.408			
Pyridine	0.139	0.094	0.037	0.034	0.010	0.001	0.000			

## TABLE VII

# ENTROPIC CONTRIBUTION ( $\chi^\infty_S$ ) to the solute–polymer interaction parameters calculated from Eqn. 11

Mixtures of OV	Mixtures of OV-101–OV-25											
Compound	φον-101											
	1	0.831	0.589	0.410	0.397	0.268	0.084	0				
n-Hexane	0.268	0.297	0.388	0.483	0.497	0.514	0.640	0.635				
n-Heptane	0.287	0.318	0.415	0.516	0.532	0.550	0.685	0.679				
n-Octane	0.314	0.348	0.454	0.565	0.582	0.602	0.750	0.743				
n-Nonane	0.342	0.379	0.494	0.615	0.633	0.655	0.816	0.809				
n-Decane	0.370	0.409	0.534	0.664	0.684	0.708	0.882	0.874				
n-Undecane	0.398	0.441	0.576	0.716	0.738	0.763	0.951	0.942				
n-Dodecane	0.428	0.474	0.618	0.769	0.792	0.819	1.021	1.012				
Benzene	0.173	0.191	0.249	0.310	0.320	0.331	0.412	0.408				
1-Butanol	0.171	0.190	0.247	0.308	0.317	0.328	0.408	0.405				
2-Pentanone	0.208	0.230	0.300	0.373	0.384	0.397	0.495	0.491				
Pyridine	0.151	0.167	0.218	0.272	0.280	0.289	0.361	0.357				

Mixtures of OV-101-Carbowax 20M

Compound	<i>\$\$01-101</i>					
	1	0.757	0.509	0.257	0	
n-Hexane	0.264	0.502	0.634	0.684	0.609	 
n-Heptane	0.283	0.538	0.678	0.732	0.652	
n-Octane	0.309	0.588	0.742	0.801	0.713	
n-Nonane	0.336	0.640	0.807	0.872	0.776	
n-Decane	0.364	0.692	0.873	0.942	0.839	
n-Undecane	0.392	0.746	0.941	1.016	0.904	
n-Dodecane	0.421	0.801	1.010	1.091	0.971	
Benzene	0.170	0.323	0.408	0.440	0.392	
1-Butanol	0.168	0.320	0.404	0.436	0.388	
2-Pentanone	0.204	0.389	0.490	0.529	0.471	

## Mixtures of OV-225-SP-2340

Compound	φον-225									
	1	0.781	0.508	0.363	0.327	0.103	0			
n-Hexane	0.418	0.364	0.305	0.653	0.425	0.676	0.985			
n-Heptane	0.447	0.390	0.326	0.698	0.454	0.724	1.055			
n-Octane	0.489	0.426	0.357	0.764	0.497	0.792	1.154			
n-Nonane	0.532	0.464	0.388	0.831	0.541	0.862	1.255			
n-Decane	0.575	0.501	0.420	0.899	0.585	0.931	1.357			
n-Undecane	0.620	0.540	0.452	0.969	0.630	1.004	1.463			
n-Dodecane	0.665	0.580	0.486	1.040	0.677	1.078	1.571			
n-Tridecane	0.710	0.619	0.518	1.109	0.722	1.149	1.675			
n-Tetradecane*	0.755	0.658	0.551	1.180	0.768	1.223	1.782			
n-Pentadecane*	0.803	0.700	0.586	1.255	0.816	1.300	1.895			
Benzene	0.269	0.234	0.196	0.420	0.273	0.435	0.634			
1-Butanol	0.266	0.232	0.194	0.416	0.271	0.431	0.628			
2-Pentanone	0.323	0.282	0.236	0.505	0.328	0.523	0.762			
Pyridine	0.235	0.205	0.172	0.367	0.239	0.381	0.555			

#### TABLE VIII

Solute	$\chi_H^\infty$	$\chi^{\infty}_{S}$				
		Eqn. 10	Eqn. 11	-		
n-Hexane	0.238	0.171	0.497		 ,	
n-Heptane	0.109	0.468	0.532			
n-Octane	0.063	0.626	0.582			
n-Nonane	0.028	0.753	0.633			
n-Decane	0.009	0.855	0.684			
n-Undecane	0.001	0.936	0.738			
n-Dodecane	0.0004	1.006	0.792			
Benzene	0.103	0.187	0.320			
1-Butanol	1.009	0.472	0.317			
2-Pentanone	0.063	0.570	0.384			
Pyridine	0.606	0.046	0.280			

ENTROPIC CONTRIBUTION TO THE SOLUTE-POLYMER INTERACTION PARAMETER FOUND WITH EQNS. 10 AND 11 FOR OV-101/OV-25 = 0.397:0.603

differences between the values found for  $\chi_s^{\infty}$  by the two procedures. Perhaps values derived from the intercept of eqn. 11 (Table VII) are less reliable than those found from eqn. 10. The reason might be that the range of values of solubility parameters of solutes,  $\delta_1$ , used is small (5.8–9.7) and extrapolation to  $\delta_1 = 0$  is not very precise.

As predicted by Flory<sup>35</sup>, it may be found that  $\chi_{\rm H}^{\infty} < \chi_{\rm S}^{\infty}$  with values of  $\chi_{\rm H}^{\infty}$  that are small for solutes and polymers of similar chemical structure (values of the solubility parameters of the same order). From the results shown in Table VI it may be observed that, as expected,  $\chi_{\rm H}^{\infty}$  values for *n*-alkanes in OV-101 are rather small, increasing as the mixed stationary phase becomes more and more polar (the proportion of the polar component increases in the mixed stationary phase). On polar polymers, polar substances show small values of the enthalpic contribution to the interaction parameter (benzene in OV-225 or OV-25; pyridine in SP-2340). When the "polarities" of the solute and polymer are dissimilar, the value of the enthalpic contribution becomes more important. Thus it may be observed that  $\chi_{\rm H}^{\infty}$  values are larger than  $\chi_{s}^{\infty}$  values for the polar solutes in apolar stationary phases or *n*-alkanes in systems such as that of the cyanosilicones. In all instances of solute-polymer similarity,  $\chi_s^{\infty}$  should be more important than  $\chi_{\rm H}^{\infty}$ , and the contrary should be expected in instances of dissimilarity. The values of  $\delta_1$  and  $\delta_2$  may give an idea of the relative values of  $\chi_H^{\infty}$  and  $\chi_{s}^{\infty}$ . However, the prediction of the value of the solute-polymer interaction parameter,  $\gamma^{\infty}$ , does not seem possible from a knowledge of the two solubility parameters.

The concept of  $\chi_s^{\infty}$  is ambiguous and it probably indicates the importance of the interaction of the solute molecule with the polymer in the ordering of the system<sup>36</sup>. It must be considered as a correction factor and probably should be further corrected to take into account pressure-volume effects<sup>20</sup>:

$$\chi^{\infty} = \chi^{\infty}_{\rm H} + \chi^{\infty}_{\rm S} + \chi^{\infty}_{\rm PV} \tag{12}$$

# TABLE IX

# POLYMER-POLYMER INTERACTION PARAMETER, $\chi^{'}_{2,3}$ , AT 393 K

Compound	<i><b>Qov</b>-101</i>	<i>Фог</i> -101								
	0.831	0.589	0.410	0.397	0.268	0.084				
n-Hexane	0.423	0.340	0.180	0.230	0.423	-0.182				
n-Heptane	0.417	0.348	0.184	0.243	0.425	-0.146				
n-Octane	0.495	0.348	0.189	0.254	0.444	-0.131				
n-Nonane	0.479	0.367	0.214	0.260	0.437	-0.120				
n-Decane	0.474	0.385	0.232	0.280	0.464	0.014				
n-Undecane	0.517	0.398	0.229	0.298	0.474	0.042				
n-Dodecane	0.548	0.399	0.234	0.304	0.486	0.110				
Benzene	0.175	0.136	0.061	-0.035	0.009	-0.453				
1-Butanol	0.285	0.054	0.021	-0.123	-0.046	-0.856				
2-Pentanone	0.489	0.133	0.062	-0.117	0.196	-0.358				
Pyridine	-0.637	0.247	0.226	-0.122	-0.024	-0.371				

Mixtures of OV-101-OV-25

Mixtures of OV-101-Carbowax 20M

Compound	<i>Qov</i> -101	ı			
	0.757	0.509	0.257		
n-Hexane	0.476	0.503	0.582	 	
n-Heptane	0.603	0.667	0.859		
n-Octane	0.600	0.751	0.969		
n-Nonane	0.675	0.845	1.163		
n-Decane	0.718	0.914	1.330		
n-Undecane	0.817	1.039	1.506		
n-Dodecane	0.877	1.144	1.670		
Benzene	-0.651	-0.409	-0.636		
1-Butanol	-0.378	0.063	0.159		
2-Pentanone	-0.906	-0.555	-0.534		

## Mixtures of OV-225-SP-2340

Compound	φον-225					
	0.781	0.508	0.363	0.327	0.103	
<i>n</i> -Hexane	1.559	1.939	1.212	1.466	2.189	
n-Heptane	1.666	2.037	1.330	1.647	2.336	
n-Octane	1.796	2.111	1.467	1.775	2.514	
n-Nonane	1.851	2.225	1.593	1.862	2.593	
n-Decane	1.905	2.319	1.681	1.995	2.654	
n-Undecane	2.052	2.447	1.866	2.136	2.843	
n-Dodecane	2.141	2.550	1.957	2.265	3.132	
n-Tridecane	2.234	2.652	2.082	2.408	3.094	
n-Tetradecane*	2.331	2.749	2.210	2.534	3.178	
n-Pentadecane*	2.418	2.844	2.323	2.646	3.222	
Benzene	0.729	1.146	0.449	1.207	1.646	
1-Butanol	0.744	1.151	0.555	1.214	1.990	
2-Pentanone	0.918	1.433	0.182	1.683	1.624	
Pyridine	0.786	1.145	0.344	1.197	1.979	

## The polymer-polymer interaction parameter

The polymer-polymer interaction parameters have been presented previously<sup>12</sup> for the three systems studied here. The values, deduced according to Perry and Tiley<sup>7</sup>, are mean values for all *n*-alkanes and stationary phase compositions, including single stationary phases. The value corresponding to each solute on every mixed stationary phase may be deduced according to the expression<sup>15,16,37</sup>

$$\chi_{1,(2,3)}^{\infty} = \chi_{1,2}^{\infty} \varphi_2 + \chi_{1,3}^{\infty} \varphi_3 - \chi_{2,3}^{\prime} \varphi_2 \varphi_3 \tag{13}$$

where all the symbols have the usual meanings and  $\chi'_{2,3}$  is the polymer-polymer interaction parameter normalized for the size of the solute molecule ( $\chi'_{2,3} = V_1^0\chi_{2,3}/V_2^0$ ). In this way, values of  $\chi'_{2,3}$  are obtained for each probe and mixture composition. Table IX presents the results obtained. It may be observed that the value of  $\chi'_{2,3}$  depends on both the solute and mixture composition. This effect has been observed in the past<sup>37</sup>.

The dependence of the value of the polymer-polymer interaction parameter on the chemical structure of the solute is a common phenomenon, although not allowed by theory<sup>32</sup>. It has been interpreted as arising from the preferential interaction with one of the two types of polymer segments<sup>38</sup>. Olabisi<sup>39</sup> attributed this to the non-random distribution of the solute in the stationary phase owing to its preferential affinity for one of the components. Selective solutes do not "sense" the three varieties of intramolecular contacts in the polymer mixture (A-A, A-B, B-B) in proportion to concentration. Instead, they detect a relatively low concentration of the chains for which they are non-solvents. This modifies the retention volume (and  $\chi'_{2,3}$ ) values relative to those which would be obtained by a truly random mixing of the solute with the polymer<sup>38</sup>. Less selective solvents, on the other hand, exhibit a more random "sampling" of the molecular environment of the stationary phase owing to the equal affinities they have for both. It is therefore expected that a better measure of the polymer-polymer interaction will be likely with less selective solvents. According to these ideas, solutes with different chemical structure should behave differently in a mixture of two "different" polymers, i.e., polymers of very different "polarity". Accordingly, one type of solute may behave in such a way that they show a "linear behaviour with mixture composition" when specific retention volumes are considered, whereas other types of solutes might not show the same type of linear dependence on mixture composition, when the same mixture is considered in both instances.

MEAN VALUES OF $\chi'_{2,3}/V$	<sup>0</sup> FOR <i>n</i> -A	LKANES AT 393 K
System	a*	b**

System	a*	b**			
OV-101-OV-25	1.59	1.42	 		
OV-101-Carbowax 20M	4.39	4.33			
OV-225–SP-2340	9.02	9.79			

\* Values obtained according to Perry and Tiley<sup>7,12</sup>.

\*\* This work.

TABLE X

In order to compare the values of the polymer-polymer interaction parameter obtained in this paper based only on mixed stationary phases with those found previously for the same systems using both single and mixed stationary phases, we calculated the average value of  $\chi'_{2,3}/V_1^0$  corresponding to all *n*-alkanes in all mixed stationary phases. The values are compared with those obtained previously<sup>12</sup> in Table X. The figures corresponding to each system are not exactly the same because in the present instance only mixed stationary phases could be considered.

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